

$$\textcircled{1} \quad \gamma m \left( \ddot{x} - \frac{v_s^2}{r} \right) = -q v_s B_y$$

$$\gamma m \ddot{y} = q v_s B_x$$

$$\gamma m \left( \ddot{x} - \frac{v_s^2}{R(1+\frac{x}{R})} \right) = -q v_s B_0 \left( 1 + \frac{B_{yx} x}{B_0} \right)$$

$$\gamma m \ddot{y} = q v_s B_0 \frac{B_{yx}}{B_0} y \quad \rightarrow \quad q v_s B_0 = \frac{\gamma m v_s^2}{R}$$

$$q B_0 = \frac{\mu_0}{R} = \frac{\gamma m v_s}{R}$$

$$\ddot{x} \left( -\frac{v_s^2}{R} \right) + \frac{v_s^2}{R^2} x = \left( -\frac{v_s^2}{R} \right) - \frac{v_s^2}{R} \frac{B_{yx} x}{B_0}$$

$$\ddot{y} = \frac{v_s^2}{R} \frac{B_{yx}}{B_0} y$$

$$B_y = B_0 \left( \frac{R}{r} \right)^n \quad \ln B_y = \ln B_0 + \ln \left( \frac{1}{1+x/R} \right)^n$$

$$= \ln B_0 - n \ln \left( 1 + \frac{x}{R} \right)$$

$$\frac{dB_y}{B_0} = -n \frac{dx}{(1+x/R)R} \Big|_{x=0}$$

$$\frac{dB_y}{dx} = B_0 \left( -\frac{n}{R} \right) = B_{yx} = B_{xy} = -\frac{B_0 n}{R}$$

$$\ddot{x} + \frac{v_s^2}{R^2} (1-n) x = 0$$

$$\ddot{y} + \frac{v_s^2}{R^2} n y = 0$$

$$\frac{v_s}{R} = \omega \text{ frequency of revolution}$$

$$\textcircled{5} \quad M_F = \begin{pmatrix} \cos & \frac{1}{\sqrt{R}} \sin \\ -\sqrt{R} \sin & \cos \end{pmatrix} \quad \begin{array}{l} \text{All args.} \\ \text{are } \sqrt{R} L \end{array}$$

$$M_d = \begin{pmatrix} \cosh & \frac{1}{\sqrt{R}} \sinh \\ \sqrt{R} \sinh & \cosh \end{pmatrix}$$

$$M_F M_d = \begin{pmatrix} \cosh \cos + \sinh \sin & \frac{\sinh \cos + \cosh \sin}{\sqrt{R}} \\ \sqrt{R} (\sinh \cos - \cosh \sin) & \cosh \cos - \sinh \sin \end{pmatrix}$$

$$\left| \frac{1}{2} \text{Tr} (M_F M_d) \right| = \left| \cosh \cos \right| < 1$$