AIR EXCHANGE MEASUREMENTS IN A HIGH-RISE OFFICE BUILDING

by

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Air exchange rates were measured in the tower of an 11-story office building using SF₆ as a tracer gas. Inside-outside pressure difference measurements were also monitored as a function of temperature and wind speed. Fall and winter air exchange rates, I (hr⁻¹), measured with make-up and main exhaust pathways blocked could be represented as a function of wind speed, W (mi/hr), by the equation

\[ I = 1.08 + 0.036W - 0.0005W^2, \quad \sigma = 0.15. \]

Wind direction and temperature difference (stack effect) exerted little effect on air exchange rate. In this building, toilet exhausts and other weather independent mechanisms were more important than natural infiltration in producing air exchange. Also, a preliminary analysis of predicted air infiltration by the Shaw-Tamura model was undertaken. The results of this preliminary analysis were consistent with the observations that the stack effect was unimportant and that natural infiltration contributed only part of the total air exchange. However, the plot of calculated infiltration rate as a function of wind speed, using the Shaw-Tamura model, had a different form from the plot of measured data.

INTRODUCTION

It has been estimated that the operation of commercial buildings in the United States uses approximately 5.5 million barrels of oil a day [1]. Office buildings as well as other buildings with central heating and cooling and forced air ventilation comprise a major segment of this building stock. Air exchange is an important component of energy usage. However, in the development of conservation measures and the design of new buildings, less is known about the losses due to air infiltration and other mechanisms of air exchange in large buildings than in single-family residences.

It is fair to say that large office buildings differ from single-family residences not merely in scale but in the complexity of their ventilating systems, which are custom designed for each building. A home may have a single ventilation system or none at all; a large building may have several, each serving a different zone. A home usually depends on infiltration for ventilation; a large building has both infiltration and forced-air intakes and exhausts. The air exchange rate of a large office building is the result of a composite effect of wind, inside-outside temperature difference and the building ventilation system. The present study attempts to measure and interpret the effects of these components.

The most extensive analyses of air exchange in high-rise buildings to date are those of Tamura and others at the National Research Council of Canada [2-10]. Jackman [11], and Barrett and Locklin [12] have also contributed analyses of this subject. Cockroft [13] and deGids [14] have developed analyses of flows and air exchanges in buildings, but these latter analyses were not primarily oriented toward tall buildings. The paper by Shaw and Tamura [9] is of particular interest, because it develops a comparatively simple computational scheme for calculating infiltration rates of tall buildings. However, it is based on wind tunnel measurements of models and determination of the average flow resistance of the building envelope by pressurization measurements. It has been compared with tracer gas measurements of infiltration rates of houses [15] but not for large buildings. Tracer gas measurements of large buildings have been made [17-19], but attempts to correlate them with computational models are at an early stage.

This paper reports experimental measurements of the ventilation of an 11-story office building by tracer gas techniques and correlation of the results with concurrent weather
data and inside-outside pressure difference measurements. The ultimate purpose of such measurements is to be able to test computational models of air exchange in large buildings, such as the model of Shaw and Tamura [9], and to aid the development of improved models. This study is also a test of measurement methodology.

DESCRIPTION OF BUILDING AND ITS VENTILATION SYSTEM

The measurements described in this paper were made in the Administration Building of the National Bureau of Standards. It is an eleven-story office building surrounded by low-lying buildings and open space. A view of the building is shown in Figure 1. A schematic representation of the main features of the building and its ventilation system is shown in Figure 2. Floors two through eleven, referred to as the tower, were the primary focus of this study. These are served by four air handling units located in the mechanical equipment room which occupies the mezzanine between the first and second floors. These units are designated as 3, 4, 5 and 6. All four of the units supply air to part of each floor of the tower as shown in the schematic diagram in Figure 3. Unit 3 serves the west end of each floor, and unit 6 the east, while 4 and 5 serve the north and south sides, respectively. Return air from floors 7 through 11 comes back through air handling units 3 and 4, while return air from the rest of the tower goes to units 5 and 6. Thus the ventilation system provides for distribution and mixing of air throughout the tower.

The main air supplies to the tower are summarized in Table 1. These estimates were based on anemometer scans of the downstream faces of the filters. They indicate a total volume of air moved within the building equivalent to 4.5 air changes per hour (hr⁻¹). A typical estimate of outside makeup air was approximately 0.3 hr⁻¹. However, makeup air dampers can modulate the rate of air intake. To eliminate the possibility of variation of makeup air and to permit operation with recirculated air, special frames covered with sheets of polyethylene were installed in each air handling unit. A door was built into each frame which could be opened to permit normal operation of the system or closed to block makeup air. The relief (exhaust) vents were also blocked during air exchange measurements. The points of blockage are shown in Figure 3. Except where otherwise stated all measurements were made with makeup and relief (exhaust) vents of each air handling unit blocked.

In addition to the main air flows indicated in Table 1, toilets and elevators were vented to the roof. There were also exchanges with the mechanical equipment room through the small grille in the return loop shown as S in Figure 3. This grille is present in three of the four units. When the make-up and relief (exhaust) vents were blocked, the grilles of two of the units acted as intakes, because the supply fan delivered more air than the return fan. Toilet, elevator and mechanical equipment room air exchange rates are summarized in Table 2. Air was diverted to the first floor from units 3 and 4 and this too is listed in the table. The effect of the foregoing flows, as well as exchanges with other parts of the building and losses through the stairwell exhausts (which were turned off), have not been independently quantified, but they are assumed to provide a nearly constant component of the air exchange rate in addition to infiltration.

Besides the mechanical system the dimensions of the building provide important parameters of the ventilation system. The base dimensions of the tower are 220 ft x 44 ft (67 x 13m) and the height, excluding the penthouse, is 102 ft. (31 m). This corresponds to a gross volume of 990,000 ft³ (28,000 m³). Allowing fifteen per cent of the volume for inside walls, partitions and furnishings results in an estimated net volume of 840,000 ft³ (24,000 m³). This estimate has been used for converting volume flow rates to air changes per hour and vice versa. The envelope area of the tower, including top and bottom surfaces, is estimated to be 73,000 ft² (7,200 m²).

EQUIPMENT AND METHODS

Sulfur hexafluoride (SF₆) tracer gas concentrations were measured with a small chromatograph equipped with an electron capture detector, an internal sampling pump and rotary sampling valve. A timer-controlled system of valves and an auxiliary pump were used to draw air to the chromatograph probe from different parts of the building in timed sequence. This sampling system is a compact modification of one previously described [20, 21].

Tracer gas was simultaneously fed into the return fans of the four air handling units through four polyethylene tubes of equal length diverging from a flow divider. A similar
system was used to sample air. After introduction of tracer gas, and allowing several minutes for the ventilating system to distribute it throughout the building, samples were taken at eight-minute intervals and analyzed for SF₆. When the tracer gas decay rate stabilized, air exchange rate was determined from the slope of the decay plot according to the equation

\[ I = \frac{-1}{t} \ln \frac{c}{c_0} \]  

where

- \( I \) = air exchange rate in air changes per hour (hr⁻¹)
- \( c \) = tracer concentration after elapsed time \( t \)
- \( c_0 \) = initial tracer concentration at arbitrarily selected time \( t = t_0 \)
- \( t \) = elapsed time in hours.

In special tests, average air exchange rates obtained by separately analyzing the individual air handling units agreed within 0.01 hr⁻¹ with the value obtained from the composite samples from the flow divider. A similar average based on twelve sample series taken at local sites of different floor levels throughout the building agreed within 0.05 hr⁻¹ with the average of the composite samples, although individual deviations as large as 0.4 hr⁻¹ were observed. Also, tracer gas decay rates at the local sites required ten to fifteen minutes longer to stabilize than those obtained from the air handling units.

Inside temperature measurements were made with a thermocouple mounted in the return of Air Handling Unit 6. This was supplemented by thermometer measurements in the halls and stairwells at the second and eleventh floor levels on occasions when the main fans were off. Outside temperature measurements were made with a shielded thermocouple located on the north side of the building at the level of the mechanical equipment room between the first and second floor.

Inside-outside pressure measurements were made on the north side of the building with probes at the second and eleventh story levels as indicated in Figure 2. Pressures were transmitted to a variable capacitance gauge in the mechanical equipment room through 1/4 in. (6 mm) i.d. polyethylene tubing similar to that used in tracer gas measurements. The two tubes from the eleventh floor were run side by side down a stairwell to minimize temperature differences between them. Outside probes were shielded with 3-liter cylindrical enclosures with several perforations. These were designed to damp velocity pressure. They also served to keep water out of the lines during bad weather.

Wind speed and direction were measured by a sensor 12 ft (3.7 m) above the north face of the penthouse. Off-site wind measurements were obtained from National Climatic Center data taken at National Airport, located about 22 miles (35km) southeast of the National Bureau of Standards site. All correlations are based on data from the north sensor.

**TRACER GAS MEASUREMENTS**

Air exchange rates with intakes and exhausts of the four air handling units blocked were measured under a range of wind and temperature conditions. The results are shown in Figure 4, where air exchange rate is plotted against inside-outside temperature difference. The figure is subdivided into a number of fields in order to examine different wind-speed ranges separately. It was found that air exchange rate showed very little temperature dependence even at low wind speeds when the effect would be expected to be greatest. Obviously there should be significant stack pressures in a building of this height, so this behavior needs some explanation.

It has been well-established in single-family residences that above certain wind speeds infiltration rate is wind dominated [22, 23, 24]. The modeling analysis of a tall building by Jackman [11] predicted that the combined effect of wind and stack effect at 10 and 20 mi/hr would have been scarcely different than the effect of wind alone. Also the analysis of Sinden [24] shows that the combined wind and stack effect should be subadditive. Likewise the “box” experiments of Blomsterberg and Harrje [26] have demonstrated mechanisms whereby the wind pressures and stack pressures can either interfere with or reinforce each other, depending upon location of the openings. In an exposed building wind effects would be maximized.
The ratio of the lateral surface area to the cross-sectional area of the building was about 5.5 to 1. As building height increases, lateral surfaces over which stack pressures must compete with wind pressures are increased, while internal vertical pathways are proportionally smaller than in single-family residences. In the Administration Building stairwells and elevator shafts comprise less than six percent of the cross-sectional area, and these are accessible only through normally closed doors. According to Jackman's analysis [11] stairwell doors should reduce air infiltration due to stack effect. Thus there are a number of factors which may contribute to weak temperature dependence.

Treating the data as a function of wind velocity alone, a least squares plot of the form shown in Figure 5 is obtained. A curve corresponding to a three-parameter model provides the best fit over the range of data collected. This curve levels off with increasing wind speed. These measurements were made between early October 1978 and February 1979 and thus include fall and winter data. Wind direction has also been disregarded in obtaining the best fit in Figure 5. Average deviations from best fit according to wind direction were

- North: +0.03 hr⁻¹
- South: -0.04
- East: -0.08
- West: +0.04

These are less than the normal scatter of data about the regression line. Wind tunnel measurements have demonstrated pressure differences over the surfaces of scale models of tall buildings [9, 10], and similar differences have been measured with actual buildings [27]. However, the data obtained here suggest that the linkage between wind direction and air exchange rate is weak. Others have noted this in measurements of single-family residences [28, 30].

The effect of occupancy on average air exchange rate was negligible, but there was some evidence that closed office doors on weekends impeded the distribution of tracer gas.

INSIDE-OUTSIDE PRESSURE DIFFERENCES

After observing the effect of wind and temperature difference on air exchange rate, it is of interest to note their effect on inside-outside pressure difference. The pressure response is made up of an average inside-outside pressure difference plus a fluctuating component. This is illustrated in Figure 6 where tracings of differential pressure vs time at two floor levels and two wind speeds are shown. The pressure difference due to buoyancy of the warmer indoor air (stack effect) is altered by wind, and a pulsed response is also produced. The pulsed response has been previously reported [29, 30].

Average Pressure Difference and Temperature Difference

Average inside-outside pressure difference was plotted as a function of inside-outside temperature difference in Figure 7. The total pressure difference, \( \Delta P_T \), is given by:

\[
\Delta P_T = \Delta P_{11} - \Delta P_2
\]

where

- \( \Delta P_T \) is total pressure difference
- \( \Delta P_{11} \) is inside-outside pressure difference at the i-th floor, i=2, 11
- \( \Delta P_2 \) is usually, but not always, opposite in sign, so that \(|\Delta P_T|\) is usually larger than \(|\Delta P_{11}|\) or \(|\Delta P_2|\).

Pressure probes were located on the north side of the building, so Figure 7 includes the responses to wind from the windward, leeward or lateral directions at different times. Wind directions have been divided into 90-degree quadrants, and designated in the figure by identifying symbols.

Referring to Figure 7, the sloped line in each field is an approximation of the total pressure difference due to pure stack effect. At wind speeds of 0-5 m/ hr (0-2.2 m/s) the estimated and measured total inside-outside pressure differences were in approximate agreement. It should be noted here that the net contribution of the main ventilating system...
to the pressure difference with intakes and exhausts blocked and the toilet exhaust in
operation was less than 0.01 mm Hg (1.3 Pa). At higher wind velocities the simple corre-
lation between inside-outside temperature and pressure was lost. This is consistent with
the observation that there was no correlation between temperature difference and air exchange
rate. However, at wind speeds less than 5 mi/hr (2.2 m/s) pressure difference showed
stronger coupling with inside-outside temperature difference than did air exchange rate,
possibly because natural infiltration was only part of the total air exchange rate.

Average Pressure Difference and Air Exchange Rate

Fig. 8A shows air exchange rate as a function of $\Delta P_1$, and Fig. 8B as a function of $\Delta P_2$.
From Fig. 8A it is seen that at the eleventh floor level 1) the average inside pressure
was always larger than the outside pressure, 2) the effects of wind direction were lost,
and 3) the curve levels off at increasing air exchange rates in a somewhat similar manner
to Figure 5. At the second floor, as seen in Figure 8B, there were clear directional
effects, probably because the probe was more protected from downsweep and lateral air currents
due to southerly winds than the probe nearer the top of the building. Due to the location
of the sensors on the north side of the building, when the wind blew from the north, inside
pressure always registered less than outside pressure. When it blew from the south, the
opposite was true. When it blew from the west the inside-outside pressure relationship
could shift either way. Thus the wind patterns were different at the two levels, but the
difference in air exchange rates were only slightly different regardless of wind direction.

Air flow through a building envelope by fan pressurization or evacuation may
may be expressed by the equation

$$Q = kA(\Delta P)^n$$

where

Q = flow rate
k = flow coefficient
A = area of the building envelope
n = flow exponent

For this calculation $k = 0.9 \text{ cfm ft}^2$, or $1.3 \times 10^{-4} \text{ m}^3 \text{ Pa}^{0.65}$

$A = 73000 \text{ ft}^2$ (7200 m$^2$), $n = 0.65$. The source of these values is given in the section
on Equipment and Methods and in the Appendix).

Equation 3 has been converted to air changes per hour and plotted in Figures 8A and
B in order to compare projected air exchange rate due to fan pressurization or evacuation,
with observed values. It is clear that at low pressure difference measured air exchange
rate was much larger than would be predicted from uniform pressurization of the building
envelope.

Referring to Table 2, the sum of the various exhaust air flows is sufficient to account
for the rather large air exchange rate at low wind speed indicated in Figures 8A and B.
However, if this loss were made up by flow through the building envelope there should be
a corresponding inside-outside pressure difference about 0.1 mm Hg (13 Pa). This difference
was not observed, from which it is hypothesized that the loss was made up through unidentified
pathways in the mechanical ventilation system rather than by enhanced leakage through the
building envelope. The neutral zone of the building lies somewhere below the third floor
level, which supports this view. A fan system for pressurizing large buildings is under
construction. Perhaps by selectively pressurizing parts of the building it may become possible
to identify the leakage paths.

Average Pressure Difference and Wind Speed

In Figure 9A the average inside-outside pressure differences at the second and eleventh
floors are plotted as a function of wind speed. Only data obtained with northerly wind
were used in this plot in order to compare it with impact pressure calculated from the
equation
where \( P_v = 0.000901W^2 \) (4)

where \( P_v = \) velocity pressure, mm Hg \\
\( W = \) wind speed, mi/hr

(If \( P_v \) is in Pascals and \( W \) is in m/s, 0.000601 is substituted for 0.000901)

This comparison is of interest, because it is often assumed that the driving pressure in air infiltration is proportional to \( W^2 \) [4, 14]. According to Figure 9A, this assumption may tend to overestimate the pressure difference, particularly at higher wind speeds. The data also display considerable scatter, perhaps due to superimposed temperature effects, and because wind may vary over a \( \pm 45^\circ \) range. Also, the effect of turbulence and the action of the fluctuating pressure component on the average pressure difference are not fully understood.

Pressure Difference Fluctuations

The fluctuating component of inside-outside pressure difference increased with wind speed, as shown in Figures 9B and C where the average amplitude of the pressure fluctuations, \( \Delta F_2 \) and \( \Delta F_{11} \), are plotted against wind speed. Equation 4 is included in the plot for comparison. The relationship between \( \Delta F \) and wind speed could be better approximated by a straight line than by the equation. It has not been established whether the average pressure difference or the fluctuating component or a combination of the two is the primary driving force in infiltration, but according to data presented here neither average nor the fluctuating component varies as \( W^2 \).

The relationship between air exchange rate and pressure fluctuations is shown in Figure 8C. It is similar in form to Figures 5 and 8A and B where wind speed and average pressure difference were the independent variables.

Grimsrud, Sherman et al. [30, 31] have monitored pressure differences at several points over the surface of a house and found the integrated average pressure difference at each point to be zero. They also developed and tested an air infiltration model using the fluctuating pressure component and obtained good agreement between measured and predicted infiltration rates in many, but not all of the houses they examined. In addition to establishing the importance of pressure fluctuations, their work implied that wind direction was relatively unimportant. Potter [32] measured differential pressures at selected points across the surface of a dwelling unit in an apartment house. He obtained better agreement between infiltration rates measured by tracer gas with those estimated from pressure fluctuations than with infiltration rates calculated from time averaged pressure differences. He also found weak correlation between infiltration rate and wind direction. Thus fluctuating pressure difference as a driving force of infiltration is receiving serious attention at the present time.

WIND MEASUREMENTS

All wind speed correlations were based on data obtained with a sensor above the north face of the penthouse. Comparing these data for October, November and December with data obtained concurrently at National Airport, an average ratio of on-site to airport wind speed was found to be 0.79, \( b = 0.39 \). The average wind on-site speed was 11 mi/hr (4.9 m/s). The equation used by Shaw and Tamura [9] for relating weather station data to on-site data is:

\[
\frac{V_L}{V_S} = \left( \frac{G_S}{Z_S} \right)^{1/7} \left( \frac{H}{G} \right)^{1/3}
\]

(5)

where

\( V_L = W_L = \) Mean wind speed at top of building \\
\( V_S = W_S = \) Mean wind speed at meteorological station \\
\( G_S = \) Gradient height at meteorological station \\
\( Z_S = \) Anemometer height at meteorological station \\
\( H = \) Height of building (top of penthouse) \\
\( G = \) Gradient height at building site.
Both National Airport and the NBS sites are in locations comparatively unobstructed by tall buildings, so a gradient height of 900 ft. (274m) has been used for both G, and G. Zs is 65 ft. (20m) and H is 142 ft. (43m). Substituting these values in Eq. 5 gives:

\[ \frac{V_s}{V_s} = 0.79 \]

The close agreement between the measured and calculated ratio between wind speed at the top of the building and at the airport may be somewhat fortuitous because assumptions were used to select the gradient height at the two sites and the choice of exponents. However, the results suggest that wind speed averaged over the three months would have given acceptable agreement between the two sites using eq. 5, although on an hour-by-hour basis differences might be significant.

Wind direction was in good agreement between the two sites at wind speed greater than 10 mi/hr (4.5 m/s). At slower wind speed the differences were often large.

**SHAW-TAMURA EQUATION**

It is difficult to test the Shaw-Tamura relationships, or any infiltration model, with data obtained in this investigation, because a major part of the air exchange rate was due to building exhausts and other mechanisms independent of weather, not explicitly identified. Nevertheless, comparison of calculated and experimental results helps define the measurement and computational problems.

Air infiltration rates due to stack effect and wind calculated by the Shaw-Tamura equations are shown as curves A and B in Figure 10. Further details of the calculations are given in the Appendix. The best line fit from Figure 5 was transposed to Figure 10 as curve C for comparison. Analysis of the combined effect of wind and stack effect indicated that air exchange rate was essentially dominated by wind, and little difference would be observed if the temperature component were ignored. This is at least in qualitative agreement with experimental observations.

If it is assumed that 1.08 hr\(^{-1}\) represents the sum of all weather-independent air exchange rates, even though this rate has not been quantitatively accounted for by independent measurement, then any excess over this intercept is treated as the natural infiltration component of air exchange. When the Shaw-Tamura calculation is compared with this segment of the experimental data, the result suggests that the estimated infiltration rates may not be unreasonable. However, aside from the accuracy of the assumptions used in this comparison, the experimentally derived curve levels off while the calculated curve has a continuously increasing slope. The calculated values are lower at low wind speeds and higher at very high wind speeds. The increasing slope is somewhat reminiscent of the impact pressure curve in Figure 9, suggesting that the driving force for flow through the building envelope may not be proportional to wind velocity squared. A somewhat similar effect is shown in comparisons of measured and calculated data for two houses described by Tamura [15]. However, this point needs further consideration. Flow data of Cockcroft and Robertson [33] for air exchange rate when air is directed against a single opening in a chamber has a form at least qualitatively similar to the continuously increasing shape expected from increasing impact pressure. In addition, mobile home data by Goldschmidt et al. [34] show a dependency of infiltration rate on wind speed which is qualitatively similar to curve B in Figure 10.

**SUMMARY AND CONCLUSIONS**

Air exchange rates were measured in the tower of an eleven-story office building using SF\(_6\) as a tracer gas. Wind data as well as inside-outside temperature and pressure measurements were also obtained. The results lead to the following conclusions:

1. Fall and winter air exchange rates, I, measured with the makeup and main relief (exhaust) pathways blocked could be represented by the regression equation:

\[ I = 1.08 + 0.036W - 0.0003W^2, \sigma = 0.15 \]

where W = wind speed, hr\(^{-1}\)
\[ \sigma = \text{standard deviation hr}^{-1} \]
2. Correlation of air exchange rate with wind direction was weak.
3. Correlation of air exchange rate with inside-outside temperature difference was marginal at wind speed below 5 mi/hr (2.2 m/s) and virtually nonexistent at higher wind speeds.
4. The large intercept at zero wind speed is attributed in part to toilet exhausts and air diverted to other parts of the building. The weather independent components of air exchange rate were not quantitatively accounted for.
5. Inside-outside pressure differences displayed an average difference plus a fluctuating component, as previously noted by others.
6. Average inside-outside pressure difference was in essential agreement with theoretical stack pressure at wind speed less than 5 mi/hr (2.2 m/s), but at higher wind speed the correlation was lost. This provides a plausible explanation of why air exchange rate showed little systematic variation attributable to stack effect.
7. Weather independent air exchange rate greatly exceeded natural infiltration as calculated by the Shaw-Tamura model.
8. Measured air exchange rate as a function of wind speed began to level off at higher wind speed, while the model calls for an accelerating air exchange rate with increasing wind speed.

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The Shaw-Tamura equation for relating infiltration rate to wind speed and direction may be expressed in the form

\[ Q_w = 6.80 \times 10^{-3} \, C_w \, L \, H \, \omega \, V_t^{1.3} \]  \hspace{1cm} (A-1)

where

- \( Q_w \): flow rate at which air enters and leaves the building, cfm
- \( C_w \): average flow coefficient of building envelope = 0.9 cfm\( \text{ft}^2 \cdot \text{in Hg}^{0.65} \)
- \( L \): length of long side of building = 220 ft
- \( H \): height of building = 102 ft
- \( V_t \): wind speed at top of building
- \( \omega \): \( Q_w \) at wind angle \( \theta \)
- \( \omega_0 \): \( Q_w \) at wind angle 0
- \( \omega_1 \): \( Q_w \) at wind angle 0
- \( V_t \): wind speed at top of building, mi/hr
- \( W \): wind speed at top of building, mi/hr

(If SI units are used, 0.699 is substituted for 6.80 x 10^{-3}, and

\[ C_w = 1.3 \times 10^{-4} \frac{m^3}{s \cdot m^2 \cdot P \cdot 0.65} \]

The average flow coefficient \( C_w \) was obtained by measuring the increase in pressure when make-up air was admitted to the building. An increase in flow of 4600 cfm resulted in an increase in pressure of 0.031 mm Hg. This was a low value and could only be measured on a calm day. Also a single point does not permit experimental determination of the flow exponent, so 0.65 is used. Nevertheless, these measurements permit approximations to be made and also allow some general observations regarding application of Equation A-1.

The direction coefficient \( \omega \) was assumed to be unity. This is equivalent to treating the data as if the wind were always blowing normally against the broad side of the building. As noted in the text, linkage between wind direction and air change rate was weak. Finally, onsite rather than airport wind data were used.

The equation for calculating the stack effect has the form

\[ Q_s = C_w S \, 0.52 \gamma P \left( \frac{AT}{T_t T_f} \right) \left( \frac{8H}{n+1} \right)^n \]  \hspace{1cm} (A-2)

where

- \( Q_s \): flow rate at which air enters and leave the building due to stack effect
- \( S \): building perimeter, 528 ft
- \( \gamma \): ratio of actual to theoretical pressure difference = 0.8
- \( P \): atmospheric pressure = 14.7 lb/in^2
- \( T_t \): absolute outside temperature, R
- \( T_f \): absolute inside temperature, R
- \( T_{10} \): absolute outside temperature, R
- \( T_{10} \): absolute inside temperature, R
- \( \alpha \): flow exponent = 0.65
- \( \beta \): ratio of height of neutral zone to building height = 0.5

Other symbols are defined in connection with equation A-1. (If SI units are used, 0.0342 is substituted for 0.52 in equation A-2.)
The value of $y=0.8$ for an office building was taken from Shaw and Tamura. Comparison of inside-outside pressures with the inside probes in the halls and in the open stairwells suggests that this was a reasonable estimate. The flow exponent 0.65 was also taken from Shaw and Tamura. Exponents between 0.6 and 0.7 are quite typical. A value of $\beta=0.5$ was used. Experimental estimates of the neutral zone obtained by extrapolating a 2-point plot of $\Delta P_{1}$ vs $\Delta P_{2}$ vs elevation through the point of zero pressure difference gave an average at the 2nd floor level, but individual estimates ranged from 5th floor to below the basement. Thus, $\beta=0.5$ provides an upper estimate of the effect of air buoyancy on air infiltration rate. It should also be noted that equation A-2 is more sensitive to uncertainties in $\beta$ than uncertainties in $C_w$, but $\beta$ is the more difficult to measure.

The equation for estimating the combined effect of wind and stack action is:

$$\frac{Q_{ws}}{Q_{lr}} = 1 + 0.24 \left( \frac{Q_{sml}}{Q_{lr}} \right)^{3.3} \tag{A-3}$$

where

$Q_{ws}$ = flow rate caused by combined wind and stack action
$Q_{lr}$ = larger value of $Q_w$ and $Q_s$
$Q_{sml}$ = smaller value of $Q_w$ and $Q_s$

Table 1

Supply and Minimum Outside Air to Tower

<table>
<thead>
<tr>
<th>Unit</th>
<th>Supply air$^1$/</th>
<th>Minimum$^2$/ outside air</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>cfm</td>
<td>m$^3$/s</td>
</tr>
<tr>
<td>3</td>
<td>14,600</td>
<td>6.9</td>
</tr>
<tr>
<td>4</td>
<td>19,200</td>
<td>9.1</td>
</tr>
<tr>
<td>5</td>
<td>18,700</td>
<td>8.8</td>
</tr>
<tr>
<td>6</td>
<td>13,800</td>
<td>6.5</td>
</tr>
<tr>
<td>Total</td>
<td>66,300</td>
<td>31.3</td>
</tr>
</tbody>
</table>

Air changes per hr

4.7

0.31

$^1$/ Obtained with outside air blocked.

$^2$/ The amount of outside air can vary, but these are representative settings.
Table 2
Summary of Remaining Building Air Exhausts and Exchanges With Main Air Handling Units in Complete Recirculation Mode

<table>
<thead>
<tr>
<th>Description</th>
<th>cfm</th>
<th>m³/s</th>
<th>hr⁻¹</th>
</tr>
</thead>
<tbody>
<tr>
<td>Toilet exhausts (Fig. 2)</td>
<td>6,100</td>
<td>2.9</td>
<td>0.44</td>
</tr>
<tr>
<td>Elevator vent (Fig. 2)</td>
<td>1,500</td>
<td>0.7</td>
<td>0.11</td>
</tr>
<tr>
<td>Air diverted to first floor (Fig. 3)</td>
<td>10,000¹</td>
<td>4.7¹</td>
<td>0.72¹</td>
</tr>
<tr>
<td>Exchange with mechanical equipment room (Fig. 3)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Unit 4</td>
<td>-2,800²</td>
<td>1.3²</td>
<td>-0.20²</td>
</tr>
<tr>
<td>Unit 5</td>
<td>-1,300²</td>
<td>0.6²</td>
<td>-0.09²</td>
</tr>
<tr>
<td>Unit 6</td>
<td>890</td>
<td>0.4</td>
<td>0.06</td>
</tr>
</tbody>
</table>

¹Based on hot-wire anemometer measurement, all others based on vane anemometer measurement.
²Negative sign signifies air is drawn into ventilation system.
Figure 2. Schematic representation of the main features of the ventilation system of the NBS Administration Building tower.

Figure 3. Diagram of air movements to and from the four air handling systems of the NBS Administration Building tower.

- Damper
- Relief (exhaust) air
- FL - Floor
- S - Air to mechanical equipment room
- M - Makeup air
- B - Points of added blockage
Figure 4. Air exchange rate as a function of inside-outside temperature difference. Figure is subdivided into class intervals according to wind speed.

Figure 5. Fall-winter air exchange rate as a function of wind speed.
Figure 6. Pressure difference vs time at high and low wind speeds.
Upper chart, wind 4 mi/hr (1.7 m/s), ΔT 21°C.
Lower chart, wind 33 mi/hr (15 m/s), ΔT 21°C.
Left, Δp 2nd floor; right, Δp 11th floor.
Full scale represents -0.5 mm Hg (-67 Pa) to +0.5 mm Hg (+67 Pa).

Figure 7. Average inside-outside pressure difference as a function of inside-outside temperature difference. Figure is subdivided into class intervals according to wind speed.
Figure 8. Air exchange rate as a function of inside-outside pressure difference
A - average pressure difference at 11th floor, $\Delta p_{11}$
B - average pressure difference at 2nd floor, $\Delta p_{2}$
C - average fluctuating component of pressure difference,
$\Delta P = \Delta F_{2} + \Delta F_{11}$.

Figure 9. Inside-outside pressure difference as a function of wind speed
A - average pressure difference in response to wind from north
B - average fluctuating component of pressure difference at 11th floor, $\Delta F_{11}$
C - average fluctuating component of pressure difference at 2nd floor, $\Delta F_{2}$.
Figure 10. Comparison of measured average air exchange rate with infiltration rate calculated by Shaw-Tamura equations.

Curve A - calculated infiltration rate due to stack effect
Curve B - calculated infiltration rate due to wind (essentially equal to combined effect of wind and stack action)
Curve B' - curve B transposed with intercept at 1.08
Curve C - best fit air exchange rate vs wind speed, transposed from Figure 5.