A Multi-Gas Tracer System for Multi-Zone Airflow Measurements

M.H. Sherman, Ph.D. D.J. Dickerhoff

ABSTRACT
Tracer gas techniques are becoming widely used to measure the ventilation rates in buildings. As more detailed information is required for both energy and indoor air quality purposes, researchers are turning to complex, multi-zone tracer strategies. Both single-gas and multiple-gas techniques are being utilized, but only multigas techniques are capable of uniquely determining the entire matrix of airflows simultaneously. A national laboratory, has developed a multi-tracer measurement system (MTMS) based on a mass spectrometer to provide real-time measurement capability of time-varying interzonal flows. MTMS has been used in both single-family and multi-family buildings to determine the flow rates both between zones and between each zone and outdoors. This report will describe the development, theory, and operation of MTMS and provide examples of data from its first year of operation in an occupied and unoccupied house.

INTRODUCTION
The multi-tracer measurement system (MTMS) has been designed to make real-time, multi-zone airflow in buildings. MTMS injects a controlled amount of various tracer gases into the test space(s) and, by monitoring the resultant concentration, can estimate the relevant airflows. The system fills the twin needs for the determination of pollutant and energy transport.

This report describes MTMS, including its hardware, principle of operation, and analysis techniques. Finally, we present results selected from its first year of operation as an example of its capabilities.

Background
Tracer gases are used in a wide range of diagnostic techniques including leak detection (Singer 1987, McCoulough 1982) and atmospheric tracing (Ferber et al. 1983). One application that has had a resurgence in the last decade is the use of tracer gases to measure ventilation (i.e., airflow) in buildings (Logan and Persily 1985). Ventilation is an important process in buildings because of its impact on both energy requirements and indoor air quality - which are both topics of concern to society. Measurement of the tracer gas concentration and source emission combined with conservation laws allows a quantitative determination of the tracer transport mechanism (i.e., a measurement of the airflow).

The vast majority of the ventilation measurements made to date have involved a single tracer gas deployed in a single zone. This technique has proven very useful for buildings that can be treated as a single zone (e.g., houses) and for more complex buildings in which there are isolable sub-sections. However, as the need to understand more complex buildings has grown, tracer gas techniques that can treat multiple zones have been developed (Harrje et al. 1985). Multizone techniques recognize that not only does air flow between the outside and the test space, but that there are airflows between different parts (i.e., zones) of the test space and, in the complete case, they are able to measure these flows. Accordingly, the complexity of multi-zone measurement techniques grows at least as fast as the square of the number of zones.

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In most tracer gas measurements of airflows there are some implicit assumptions made about the measurement zone(s) and the airflow paths. It is usually assumed that the test zones can be treated as uniformly well-mixed with respect to any tracer gases and thus can be represented by a single (spatial) concentration; similarly, any injected tracer is assumed to be instantaneously well-mixed. All airflow paths are assumed to be of negligible volume, negligible time delay, and similarly well-mixed. Realities of buildings notwithstanding, we take these assumptions to be the general case for tracer gas measurements. Sections below will discuss these zonal assumptions in more detail.

Tracer gases can be used to measure the flow through a duct, flue, or vent. Depending on the measurement strategy used, however, the assumptions of well-mixed concentration and injection may not be realized and, thus, care must be taken in treating these as a simple zone.

Multi-zone Continuity Equation

The continuity equation expresses the conservation of tracer gas. In a general multi-zone environment, a matrix form of the continuity equation must be used:

$$\mathbf{V} \cdot \mathbf{C}(t) + \mathbf{Q}(t) \cdot \mathbf{C}(t) = \mathbf{S}(t)$$  \hspace{1cm} (1.1)

For every zone of the system there will be a row in both the concentration and source-strength matrices. For every unique tracer gas there will be a column in those matrices. If there are $N$ zones, the volume and airflow matrices will be square matrices of order $N$ and the continuity equation can be rewritten with explicit indices:

$$\sum_{j=1}^{N} \left( V_{ij} C_{ij}(t) + Q_{ij}(t) C_{jk}(t) \right) = S_{ik}(t)$$  \hspace{1cm} (1.2)

In MTMS there are as many tracer species as there are zones. (Such a problem is called mathematically complete and normally yields a unique answer. See Sherman [1989] for more details.)

Equation 1 contains measured data and derived quantities. The measured data are the flows and concentrations of each tracer gas in each zone. Specifically, $\mathbf{C}_{ij}$ represents the respective value of the $j$th tracer gas in the $i$th zone. The flows to and from outside are implicit in the matrix and can be found by summing a row or column appropriately; often the matrix is expanded to include this value as a zeroth row and column. In MTMS the volume matrix is diagonal and contains the zone volumes.

The interpretation of the airflow matrix requires a bit more explanation. The diagonal elements, $Q_{ii}$, represent the total flow out of that zone to all other zones and should have a positive sign. The off-diagonal elements represent the flows between zones; specifically, $-Q_{ij}$ is flow from the $j$th zone to the $i$th zone. Since the flow from the $j$th zone to the $i$th zone can be different from the flow from the $i$th zone to the $j$th zone, this matrix will in general not be symmetric.

The flow matrix explicitly contains information about flows between measured zones and the total flow. If there are flows to zones other than those being measured (e.g., outside), the sum of some rows and columns of the flow matrix will be positive; and system is said to be open. If all zones of the building are monitored these flows to "elsewhere" are attributed to air exchange with the outside.

**MTMS PRINCIPLES OF OPERATION**

MTMS, like all tracer gas ventilation-measuring systems, uses the dilution (or non-conservation) of a tracer gas to infer airflows. In order to do this the system must be able to perform certain functions: injecting controlled amounts of tracer gases into specified zones, measuring the concentration of the tracer gases in all the zones, and storing the resultant information for later use. MTMS is able to do these functions using a PC-controlled data logging and control system.

* If, however, there is short circuiting (i.e., direct transfer without mixing) of the tracer source from one zone to another, it can manifest itself as an off-diagonal volume element, but the sum of each column must be equal to the (effective) physical volume of the zone. As such behavior is a manifestation of imperfect mixing, it is not treated in MTMS.
Control Strategy

Under perfect conditions almost any method of injecting the tracer gases into the zones would lead to a good estimate of the airflows (i.e., any method that avoids a singular concentration matrix will work). In a real situation, however, the accuracy and precision of the airflow calculation depends on many factors: instrument capabilities, relative size of airflows, mixing, the conditioning of the concentration matrix, etc. The purpose of the control algorithms in MTMS is to minimize the uncertainty in the data analysis by suitable control of the injected flow (i.e., by increasing the determinant of the concentration matrix). The subject of optimal control is, of course, an entire discipline (see, for example, Bryson and Ho 1975) and will not be described herein. The control strategy used in MTMS is an attempt to minimize errors due to several different sources as follows:

Instrumentation Accuracy: The precision of the injection and concentration determination is usually an absolute value expressed as a percentage of full scale. To minimize the impact this uncertainty has in the calculation it is desirable to maximize the signal (i.e., work as close to full scale as is practical).

Mixing: When tracer is injected into an idealized zone, it is completely and instantly mixed. In a real zone it takes some time for the measured concentration to reflect the zone average concentration. This kind of mixing effect can be reduced by keeping a steady injection and concentration within the zone rather than allowing the zone to fluctuate. (Other types of mixing effects such as stratification, dead zones, short circuiting, etc., require careful sampling design and cannot be dealt with by the control strategy.)

Matrix Conditioning: The analysis method includes the inversion of the concentration matrix. Uncertainties in the measured quantities and numerical errors will be amplified the more the concentration matrix is ill-conditioned. (The best-conditioned matrix would be diagonal; the worst would have a zero determinant.) Although the conditioning of the concentration matrix will to some extent, be limited by the conditioning of the problem (i.e., the airflow matrix), the control strategy should seek to keep the concentration matrix well-conditioned.

The MTMS control strategy is a compromise between these objectives. A single, unique tracer gas is injected into each zone. Thus, the concentration of that gas in that zone will be largest; if there were no airflow between the zones this would lead to a maximally conditioned concentration matrix. Given that it is not practical to inject a negative amount of tracer gas, this strategy leads to a most well-conditioned concentration matrix possible under the circumstances. For the single tracer to be injected into each zone a target concentration, \( C_t \) is chosen so as to maximize the dynamic range of the instrumentation and thus minimize the instrumentation-induced errors.

The control algorithm used in MTMS is a type of proportional-integral control scheme that separately controls the injection of each tracer gas based on the concentration of that tracer in the zone in which it is injected. In operation the change in the injection of each tracer gas is calculated from the difference between the estimated concentration and the target, and on how much the estimated concentration has changed since the last cycle:

\[
\Delta S = \frac{V}{r_i} \Delta C_i - \frac{V}{r_p} \Delta C_e \tag{2}
\]

The values of the two time constants in this equation determine the characteristics of the control. \( C_e \) represents an estimate of what the concentration will be at the end of the next cycle — should no change to the injected flow be made. \( \Delta C_i \) is the difference between the target concentration and the estimated concentration.

The integral time constant, \( r_i \), is the characteristic time for the system to reach its target concentration (e.g., from zero). The shorter this time constant is, the quicker the system will reach target and the effect of instrument error will be minimized. However, if \( r_i \) is too short the system will be unstable. Instability will set in if the time constant is too short compared to 1) the sampling rate, 2) the mixing time, 3) \( r_p \), and 4) any imaginary eigenvalues in the airflow matrix. Since instrument error is not a major problem for MTMS, we have selected a relatively long integral time constant to ensure stability. For MTMS the default value is \( r_i = 1 \) day.

The proportional time constant, \( r_p \), regulates how fast the concentration is allowed to change. The shorter this time constant is, the smoother the concentration time series will be. Since changes in concentration can cause errors when they happen faster than the mixing time, the optimal value for this time constant is the mixing time. In order to promote stability, the proportional time constant should lie between the sampling time and the integral time constant. For MTMS the default value is \( r_p = 15 \) minutes.
On-Line Analysis for Estimating Concentration

The control algorithm requires an estimated concentration to be calculated. This concentration, $C_e$, is that concentration that would occur if there were no changes made to the amount of tracer injected. Since in normal operation the concentration is slowly varying, the most obvious candidate for the estimated concentration is the current measured concentration. One reason for not using the measured value is that it is least representative when the system is farthest from steady state and thus may contribute to instability. If the airflow rates are high enough, using the measured value ignores the interactions between zones. A more important reason is that the measurement of concentration is subject to random noise caused by a variety of factors, one of which is poor mixing. Such noise will cause the control algorithm to needlessly alter the injection and magnify the concentration fluctuations.

One way to avoid these problems is to extrapolate the current estimated concentration from the previous estimated concentration and the system properties (i.e., injection rate, concentrations, and airflows) using the continuity equation. Since we, of course, do not a priori know the airflows, they must be calculated in real time from the data already taken. The disadvantage of such a procedure is that we may not be able to determine the airflow well enough to get a meaningful extrapolation.

Both these approaches have advantages and disadvantages; the optimal solution is to combine them together as follows:

$$C_e = C_m + \kappa \left( C_{est} - C_m \right)$$  \hspace{1cm} (3)

Such an approach is called Kalman filtering. In MTMS the Kalman gain, $\kappa$, is initially set to unity: as the on-line analysis is better able to estimate the airflows, $\kappa$ is steadily decreased to a minimum of 0.4. Should the analysis have difficulty determining the airflows, the Kalman gain is increased back to unity. This adaptive form of Kalman filtering helps keep the concentrations stable even when the airflows are changing.

The control algorithm of the previous section shows no indication that the system being controlled is coupled (i.e., multi-zone). Each injected tracer is controlled by its estimated concentration in a single zone. However, the coupled character appears in the calculation of the extrapolated concentration. Using Equation 1 we can find an extrapolated concentration from the current flows and previously calculated estimated concentration:

$$C_{est} = C_e + \delta t V^{-1} \left[ S - Q_e C_e \right]$$  \hspace{1cm} (4)

The required concentrations are the diagonal terms of the left-hand side.

In order to use this expression it is necessary to have an estimate of the current airflows. We make this estimate in real time using an averaged value of the concentrations and injections to get an estimate of the current airflows:

$$Q_e \equiv \overline{S - V \cdot \bar{C}}, \bar{C}^{-1}$$  \hspace{1cm} (5)

where the overbars indicate a digitally filtered value (with a one-hour time constant) of the measured quantities.

MTMS uses this on-line calculation in the control algorithm to give immediate feedback to the user in the field. The algorithm is not sufficiently accurate for a complete data analysis, necessitating an off-line analysis technique, which is described in a later section.

MTMS HARDWARE DESCRIPTION

The MTMS hardware is responsible for measuring the concentrations of all gases in all zones and for injecting tracer gases into those zones in order to effect the control strategy. The core of the system is the measurement of concentration and it is supported by plumbing and control technology. Total cost for the hardware described below (not including fabrication labor) was about $33,000. Figure 1 shows a diagram of the MTMS hardware.

Analysis of Concentrations

Accurate and timely measurement of the tracer gas concentrations is the constraint which is most demanding of the instrumentation and has required new methods. Mass spectrometers have long been used as a detector for chromatography, but until recently they have been too large and too costly for typ-
ical tracer gas analysis. Currently residual gas analyzers (RGA), quadrupole mass spectrometers, are small, reliable, and available at prices comparable to gas chromatographs. Their principal use is in process gases in vacuum, where both desired components are monitored as well as contaminants. Typical contaminants are air leaks, background oil or water, undesired chemical reactions, even some metals that might be present in the materials used for construction of the vacuum chamber.

Air coming into an RGA is ionized and the resulting positive ions are separated by their charge-to-mass ratios and directed at an electron multiplier for detection. Separation is achieved by directing the ions axially between four rods and varying an electric field on the rods at radio frequencies. A stable path is set up for one charge-to-mass ratio at one frequency and only it will emerge at the end of the rods. Tracer gas concentration is then proportional to the output current of the electron multiplier. This process must take place at low pressures, less than $10^{-5}$ torr, so that the ions within the quadrupole mass filter do not collide with other species (neutral or ionic).

When a new airstream is selected it must flush out the ionization area before its concentration can be measured. In MTMS the ion source, a hot wire, is open to all of the vacuum chamber. The chamber, with a volume of about one liter (L), is pumped with a 50 L/sec turbomolecular pump. This provides several air changes/second and ensures a fast response. Changing measurements from one gas (ion) to another within the same sample is simply a matter of changing the radio frequency.

The sample air pressure must be reduced to that required by the RGA. A multi-stage reduction in pressure is necessary to meet the pressure requirements. The first reduction is achieved by flow resistance within a small capillary tube. This reduction is limited to the pressure at which molecular flow is induced. The pressure is now reduced by expansion into a small chamber from which a small portion is allowed to expand into the RGA via an orifice; the bulk of the gas is pumped away with the vacuum fore pump. This process limits the response time by the travel time in the capillary and the flushing of the expansion chamber with the fore pump. Including the valve manifold, the overall response time of the MTMS hardware is about one second.

The oils used in the vacuum pumps are large hydrocarbons and even small amounts of their vapors that backflow and any oil that creeps along the chamber walls can give rise to ions at almost every mass of interest. This background can be reduced by one or two orders of magnitude with the use of a catalytic oil trap. An oil trap will also help to keep the electron multiplier clean.

The RGA itself has an absolute accuracy of about 1/4% of reading; however, at the pressures we are working there is electronic noise of about 20 ppb. Most tracer gases can be calibrated to ±1% down to 2 ppm, where the noise dominates the uncertainty. Gases with large backgrounds may have to be used at higher concentrations to maintain the same uncertainty, (e.g., helium at 5.25 ppm background will have a minimum uncertainty of 53 ppb). The electron multiplier is less sensitive to heavy ions and so it is necessary to use slightly higher concentrations for gases such as sulfur hexafluoride. For MTMS gases the typical target concentration (i.e., the concentration in the zone in which they is injected) are from 20 to 50 ppm to allow the non-target concentrations to be measured with some accuracy.

**Injection of Tracer Gas**

The tracer gas injection is controlled by a separate mass flow controller (MFC) for each gas. These devices measure the mass flow with a precision hot wire anemometer (or hot films) and control a needle valve to regulate the mass flow to within 1% accuracy (full scale) in a 50:1 operating range. These specifications are often exceeded in practice where one can sometimes get a 70:1 range and better low end accuracy. Response time is typically less than 10 seconds; occasionally some adjustments are necessary to the controls when changing gas type or flow range. Typically the MFC require a driving pressure of at least 5 psi, and give optimal performance at about 20 psi. This limits the selection of tracer gases to those which have sufficient vapor pressure at operating temperatures. Tanks of at least 98% purity are used, with 99.9% or better preferred. Diluted gas can also be used and is suggested for safety reasons if flammable gases are to be employed. The simple hydrocarbons typically have lower combustible limits at about 2%, thus requiring about 50 times more diluted tank gas than pure gases. This usually requires several tanks for an experiment and is inconvenient.

Tracer gas is transported to the zones via tubing from the rack of MTMS equipment. The tracer gas is often injected at multiple locations and small fans are used to make sure that mixing occurs. Poor mixing is usually the biggest source of error in the measurements. Preferably the tanks of tracer gas are stored outside, where a small leak will not interfere with the measurements and a large leak (damaged
tubing) will not cause the gas concentrations to rise above safety limits. Some tubing types are incompatible with some tracer gases, specifically, Teflon tubing and sulfur hexafluoride are a poor combination. MTMS uses quarter-inch polyethylene tubing, which has worked well with all the tracer gases used. Smaller tubing could decrease response time but the added resistance would limit the selection of tracer gases to those with sufficient pressure to ensure adequate flow.

The desired flow rate is requested by a 0 to 5 volt signal from the controlling computer. This can be manually overridden when desired. The actual flow is measured via a separate 0 to 5 volt signal.

Tracer Gas Selection

There are several factors governing the selection of tracer gases. The ideal gas is non-toxic, non-flammable, inexpensive, readily available, and easy to detect. An RGA is able to detect almost any gas, giving great flexibility but also difficulties from interfering gases. The gases selected must produce a characteristic ion. Normal air is a mixture of many compounds and the ions produced from its components may obscure desirable tracer gas ions. Several tracer gases have been identified for use, mainly from the chlorinated fluorocarbon (CFC) family. Unfortunately, CFCs do not yield a positive ion by losing one electron from the parent molecule. Their detection is accomplished via fragments such as (for R12): $\text{CF}_2\text{Cl}_2 + e^{-} \rightarrow \text{CF}_2\text{Cl}^+ + \text{Cl}^- + e^-$. Many CFCs can produce similar fragments, such as (for R114): $\text{C}_2\text{F}_6\text{Cl}_4 + e^- \rightarrow 2\text{CF}_2\text{Cl}^+ + 3e^-$. Many such fragments are possible for each gas. Some interferences can be accounted for and these gases can still be used. For example, it is desirable to use R22 and sulfur hexafluoride as tracer gases, but sulfur hexafluoride produces ions at mass 127 and 51 and the only usable mass for R22 is mass 51. The contribution of sulfur hexafluoride at mass 51 is 7.6% of its value at mass 127. When this value is subtracted from the value at mass 51 the result comes only from R22. Table 1 shows the gases (and their fragments) that have been selected for possible use in MTMS.

Helium has a relatively large background but, because it is inert and is available at low cost, it can be used at relatively high concentrations (lower limit at about 100 ppb). Helium, because it is incombustible, can also be used to measure flow through combustion devices. R22 is generally used after exhausting other choices because of the interferences. Most of the CFCs are available at only 98% purity and may have significant amounts of other CFCs mixed in. For this reason each tank must be measured to determine the contamination, and small interference corrections are usually needed for all the CFCs. Other gases of interest, such as $\text{CO}_2$ and $\text{H}_2\text{O}$, can also be monitored.

Sampling System

Air is pumped from each zone, and outside, continuously using a free piston pump to a valve manifold where one airstream is selected for measurement. The tubing and pump size were matched so that it takes 10 seconds at most for zone air to reach the analysis equipment. The same concerns that were noted for the injection tubing are again present for sampling. Additionally some adsorption may occur. This is usually only a problem at very low concentrations (ppb or less). At the concentration levels at which MTMS is used this is not a problem. It is possible to use injection tubing for sampling after sufficient flushing. The free-piston pump was selected because it is leak free and relatively quiet.

Care must be taken to prevent possible condensation or freezing of humid air (thus blocking the tubing) as it travels through cold areas. Usually this means that the tubing must all be inside the structure being monitored during cold weather. Alternatively the tubing could be heated in exposed areas. The flow rate is low enough that self-heating is not feasible without extensive insulation. Additional samples (i.e., measurements not used in the MTMS control) may be taken from other locations such as attics or ducts, or near suspected leakage sites.

Computer Data Acquisition and Controls

The various functions necessary for MTMS operation are performed via a host PC computer which communicates via serial ports to the RGA interface and a data acquisition computer. The data acquisition computer runs a simple program to interpret requests from the PC and read various voltages or temperatures, outputs the controlling voltages for the mass flow controllers, and operates the valves that select which zone is to be analyzed. Usually there is a weather tower to measure temperature, wind speed and direction, and one temperature for each zone. Other aspects may be monitored as well, such as barometric pressure and HVAC operation.
The RGA interface interprets requests from the PC and operates the RGA. It can select amplifier gain, select measurement mass, and measure the intensity of the ion signal. There are several other functions intrinsic to the RGA that can be accessed, such as selecting ionization filaments, degasing, total pressure measurement, detector choice, and electron multiplier voltage. Each nominal mass peak is measured at a series of masses which vary around the nominal mass by up to ± one-third of a mass unit. The result is curve-fitted to find the center and peak height. This procedure reduces the effects of noise and tracks whatever drift there may be in mass position. Because there may be background, either from natural sources (as for helium) or from oils, outside air is measured and any resulting peak is subtracted. All tracer gas measurements are made relative to the naturally occurring argon peak. Small changes in total pressure, due to tubing resistance or pumping efficiency, or changes due to electron multiplier efficiency drift are thus accounted for.

Overall response time is limited by the serial I/O between the PC and the RGA interface. It generally takes between 5 and 10 seconds per gas, depending on the concentration. Typically for a three-zone measurement it takes about 110 seconds to measure all four gases in all four zones (outside counts as a zone, and the argon reference counts as a gas).

After each zone has been analyzed the flow rates are estimated and new injection rates are calculated using the method described above and set via the data acquisition computer. The results are printed to the monitor and to a disk file for subsequent, more sophisticated, analysis. The analysis is not dependent on constant concentration and the injection control parameters are usually set for long (about one-hour) time constants.

MTMS DATA ANALYSIS METHOD

The analysis method used to reduce the data is considerably more complex than the on-line method used in the control algorithm. Inversion of Eq. 1 is a straightforward mathematical problem indicated by Eq. 5.* If there were no uncertainty in the measured data (i.e., the concentrations and source strength), this inversion would give the correct (and only) answer. In any real experiment, however, there will be uncertainty in the measurements due either to instrumentation errors or other random processes. Such uncertainty can be described by a probability distribution as to where the true value lies. Tarantola (1987) gives an excellent discourse on the issues related to the general problem of extracting model parameters from measured data.

In MTMS there are many sources of error which tend to confound the extraction of the airflows from the measured data. The random errors can be expressed as uncertainties in either the injected flow or measured concentrations. From these uncertainties the precision of an individual calculation of airflows can be determined (Sherman 1989a).

Because MTMS takes a large volume of data each hour there are about 30 full measurements consisting of injection rates and concentrations for each gas in each zone—the precision of an airflow estimate can be improved. The most robust method of increasing the precision is to integrate the continuity equation (Eq. 1) over a specified period and treat the airflows as constant over that period. The longer the integration time, the better will be the precision. If, however, the integration time is so long that the real airflows vary significantly, a non-negligible bias—typical of the passive ventilation measurement techniques—will be introduced (Sherman 1988). The selection of the optimal integration time constant requires some prior knowledge of the system; however, for houses without mechanical systems, this time is typically on the order of one hour.

Both the precision and accuracy of the calculated airflows can be improved by incorporating physical knowledge about the system. For example, the airflows are only defined in one direction; physically impossible signs for the airflows can be eliminated. Similarly, the high data rate allows us to restrain the rate of change of the airflows in time to physically reasonable limits. The details of the analysis are beyond the scope of this report, but can be found in Sherman (1986).

* As a practical matter simple matrix inversions are undesirable because of the available precision on most computers. Usually more robust computational methods are utilized to minimize the problems with ill-conditioned matrices. Conceptually, however, we can still speak of the inverse matrices.
Mixing and the Zonal Assumption

Virtually all tracer gas techniques for estimating airflows in buildings (MTMS included) use the **zonal assumption** that the volume of the building can be broken up into a set of zones, inside of which there is a single concentration of tracer gas. In other words, it is assumed that all flows out of a zone contain the single concentration of gases within the zone and that all incoming air (and tracer) is instantaneously mixed. Thus, a zone is characterized by its mixing properties and not its physical size or shape; a zone may be a set of rooms, a single room, or a part of a room.

The idealized condition of perfectly well-mixed zones is rarely realized in practice, but we have observed that it can be reasonably approached by using fans to stir the air within each zone. Such fans can be explicitly installed for mixing or can be part of the HVAC system in the building. MTMS has small fans to infuse the injected tracer evenly into each zone and, where practical, oscillating fans are used to mix the air within each zone. Mixing fans should not be located where they might change flows between the zones (e.g., pointed at a leakage site).

Should the mixing be insufficient, the zonal assumption will break down and errors can creep into the analysis. When the breakdown occurs concentrations at different points within the zone will have different values, varying both spatially and temporally.

If the poor mixing is caused by pockets of air having different concentrations traveling chaotically through the zone, one could assume that the concentration time-averaged over a long enough interval is the same at every point within the zone. In such a case the imperfect mixing can be treated as an extra uncertainty in the concentration measurement. In most real zones, this kind of uncertainty will be larger than the instrumental error of MTMS. We can use the high data rate of MTMS to estimate the magnitude of this uncertainty for every concentration and use that value in the analysis procedure.

Not all mixing problems can be treated as random errors. If, for example, the zone has a spatial concentration gradient (e.g., if it were temperature stratified) there is no single value of concentration that represents the zone. Even a spatial average of the concentration may not be representative. This kind of systematic error can cause a bias in the analysis, which cannot be eliminated by increasing the uncertainties. Biases can also be caused by averaging concentrations over periods longer than the characteristic time change of the airflows.

Biases in general cannot be uncovered by examining the quality of the data. However, the airflows are physically constrained to lie in certain ranges (i.e., non-negative airflows). It often happens that biases in the data cause the apparent flows to violate the physicality constraints. Such violation can be used to indicate that some sort of bias may be present. However, such biases may be present and not cause a violation of the physicality constraints. Therefore, good measurement technique should include an independent verification of acceptable mixing.

FIELD MEASUREMENTS USING MTMS

MTMS was in continual use from the completion of its laboratory debugging in fall 1987 through spring 1988. During this period the system was used in four different states covering three different regions of the country, including both single- and multi-family buildings and both occupied and unoccupied zones. The data covered below will be for occupied and unoccupied single-family houses. During this time MTMS was part of a tracer gas technique intercomparison in a multifamily building (Harrje et al. 1989) and in a study of radon dynamics in a single-family home (Hubbard et al. 1988).

Unoccupied House

The first field use of MTMS was in a wood frame bungalow-style, single-family house in Berkeley, CA. The house is made up of four zones; a bedroom, a kitchen/living area, a large storage room, and a laundry room. The laundry and storage rooms are below the rest of the house. From the layout one would not expect much direct communication between the bedroom and the storage room. These zones have volumes of 61, 243, 60, and 30 m³ and floor areas of 25, 190, 30, and 15 m², respectively. The total effective leakage area of the house was measured at 800 cm², and the major leakage between zones is expected to be around the doors that connect them. The house was built around 1935 and has a floor furnace in the living room.
The period selected for display was a period during the Christmas holidays in which the occupants were not in residence and the heating system was not in operation. Several small fans were used to ensure adequate mixing in all zones. The conditions were selected to be as benign as possible for the first test in field conditions.

Figure 2 is a plot of the measured airflows over a day-and-a-half period beginning on December 24. The measurement time constant is half an hour. Figure 2a shows the flows to the bedroom from all the other zones; Figure 2b shows the flows to the living room from all the other zones; Figure 2c shows the flows to the storage room from all the other zones; and Figure 2d shows the flows to the laundry room from all the other zones. During the first evening a door between the storage room and the laundry room was opened and was then closed around the following noon. As can be seen, the flows between the two affected zones change dramatically, but secondary effects on the other flows are also observable. It should be noted that the infiltration (i.e., flow from outside) is visibly increased when the internal resistance is lowered by opening an internal door. Furthermore, the number of air changes in the storage and laundry rooms is much higher than in the larger zones.

A small aberration in the flow may be noticed in the large step up and step down of the flow on the evening of the 24th and the morning of the 25th. Such an artifact is caused by the fact that the flow is changing faster than the time constant of the analysis (i.e., 30 minutes), which can cause a bias in the flow estimate. Around midnight another artifact can be observed. This artifact was caused by a variation in the instrument calibration induced by the pump oils; subsequent use of an oil trap eliminated the problem.

Occupied House

In January 1988 MTMS was transported to Olympia, WA for use in a two-story, single-family residence. The house is made up of three zones: three bedrooms combined for the first zone, the kitchen, dining room, and living room (with a cathedral ceiling) formed another zone, and the lower story (consisting of a study and family room) made up the third zone. These have floor areas of 66, 57, and 69 m² with corresponding volumes of 151, 165, and 158 m³. The house has a central forced-air heat pump, and was built around 1980. The leakage area of the house was measured at 1150 cm², with leakage in the HVAC duct system being 150 cm² of the total. The flow in the HVAC ducts was measured at 2100 m³/h while the heat pump was off and the fan forced on. The flow is lower than this when the head pump is on. There is a night setback of about 5°F which operates from 11 p.m. to 6 a.m. Usually the bedroom doors are closed at 11 p.m. and the bedroom window may be opened. At any time the door between the downstairs and living zones may be partly closed.

The period selected for display was typical of the 10-day period of monitoring; the building was conditioned and there was routine occupancy. Although the injection and sampling locations were necessarily less centrally located than in the unoccupied house, the normal use of the central heating system assisted in sufficiently mixing the tracers. The small mixing fans installed were often turned off by the residents and were not always turned back on.

Figure 3 is a plot of the measured airflows on January 15. The measurement time constant is half an hour. Figure 3a shows the flows from outside to all the other zones; Figure 3b shows the flows from the bedroom zone to all the other zones; Figure 3c shows the flows from the living/kitchen zone to all the other zones; and Figure 3d shows the flows from the family/study zone to all the other zones. Some trends are evident in these plots: the family arises at about 6 a.m. and opens the bedroom doors and the heating system comes on as the setback period is

The data in Figure 3 may be somewhat biased (see Sherman 1988, 1989b) if the furnace fan operation induces significant zonal airflows; such behavior may be visible in Figure 3. The data were then reanalyzed with a much shorter time constant and the results are shown in Figure 4. In this figure it is apparent that furnace operation has a significant effect on the zonal airflows; the pattern of cycling can be easily seen in all of the flows during the day. At night, however, the slow furnace cycling (because of thermostat setback), the low activity level, and the closed internal doors make the data too noisy to pick up trends with such a short time constant.

It is apparent that many of the flows are increased with fan operation. Since there are more supply than return registers, it is not surprising that the interzonal flows are increased when the fan is running. However, it is also apparent that the flows to and from outside are increased with fan operation; thus, operation of the HVAC system increases total infiltration.
The bias caused by a longer averaging time is apparent when comparing Figures 3 and 4 for those flows having a large oscillating component. The flows in Figure 3, while smoother, are significantly lower.

Validation

The field results do not constitute a validation of the MTMS system. Indeed, it is probably not useful to consider such a system validation. There is little doubt that if the assumptions of the continuity equation (i.e., the zonal assumptions) are met, an accurate measurement of the injection and concentration could yield the correct result. A validation of a carefully controlled set of zones would thus do no more than the individual validation of the components of the system that was done in the lab. A more thorough validation of the system, including its sensitivity to imperfect mixing and other biases, is beyond the scope of the present effort.

DISCUSSION

The focus of the MTMS development has been to create a portable system capable of measuring the ventilation between different zones of a multiple-zone building, and then use that system to 1) understand the physical processes associated with ventilation, 2) provide the capability of validating ventilation models, and 3) measure real-time airflows for diagnostic purposes. The focus of this report is to describe the multitracer measurement system.

Although the data sets provided herein are intended as examples, some inferences can be drawn. Because the data are recorded at short intervals, MTMS has the ability to respond quickly to changes in the airflows. Such quick response is especially important in the interzonal flows (cf. flows to outside), as they can change quickly in response to occupancy or the HVAC system. For pollutant transport concerns these interzonal flows may be more important than the outside air infiltration.

The data from the occupied house analyzed over 10 minutes, clearly show that the operation of a central, forced-air system makes significant changes in both the interzonal flows and in the infiltration into each zone. It is clear that the pressure in each zone is significantly different when the fans are running. Although in an individual zone this could either increase or decrease the infiltration into that zone, the total air infiltration into the building increases as a result of the differential pressurization. Furthermore, leakage between the ductwork and outside can also be responsible for increased infiltration. It is not possible from the data presented to ascertain how much of the excess infiltration can be attributed to each cause.

Comparison of the data analyzed with the two different time constants indicates the magnitude of the bias that can be introduced if a long averaging time is used in the analysis. Users of passive ventilation techniques must be aware-especially in multi-zone environments— that the use of long-term averaged concentration readings may give inappropriate, or even unphysical, results for flows that have a strong time dependence.

The MTMS is a tool that can answer many questions regarding ventilation in complex building environments. This report has demonstrated some of its capabilities and we anticipate future research efforts will make use of them. Ongoing efforts include the use of MTMS data to validate single-zone infiltration models (i.e., the LBL infiltration model) and multi-zone ventilation models (i.e. COMIS),* as well as to understand the influences that forced-air systems have on residential ventilation rates. In all, we anticipate that MTMS will provide a useful tool for understanding multi-zone ventilation in buildings.

ACKNOWLEDGMENTS

The authors would like to acknowledge Isaac Amarel of the Rafael-Armament Development Authority, Israel, for his invaluable assistance in the development and calibration of the RGA hardware during his sabbatical year at LBL.

*The Conjunction Of Multizone Infiltration Specialists (COMIS) being held at LBL is a joint international effort involving 8 different countries.
NOMENCLATURE

\[ C \] Instantaneous tracer gas concentration [kg/m\(^3\)]
\[ C_e \] Estimated tracer gas concentration [kg/m\(^3\)]
\[ C_{et} \] Extrapolated tracer gas concentration [kg/m\(^3\)]
\[ C_m \] Measured tracer gas concentration [kg/m\(^3\)]
\[ C_t \] Target tracer gas concentration [kg/m\(^3\)]
\[ \kappa \] Feedback gain for (Kalman) filtering [-]
\[ N \] Number of zones [-]
\[ Q \] Ventilation [m\(^3\)/h]
\[ Q_e \] Estimated Ventilation [m\(^3\)/h]
\[ S \] Instantaneous source strength of tracer gas [m\(^3\)/h]
\[ t \] Time [h]
\[ \delta t \] Time difference between measurements [h]
\[ \tau_i \] Integral time constant [h]
\[ \tau_p \] Proportional time constant [h]
\[ V \] Volume [m\(^3\)]
\[ \sigma \] Standard deviation of an airflow [m\(^3\)/h]
\[ i, j, k \] indices indicating zone [0,1 \cdots N]
\[ X \] (bold) indicates matrix of (X) values

REFERENCES


TABLE 1: MTMS TRACER GAS PROPERTIES

<table>
<thead>
<tr>
<th>GAS</th>
<th>ION</th>
<th>MASS</th>
<th>COMMENTS</th>
</tr>
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<tbody>
<tr>
<td>He</td>
<td>He⁺</td>
<td>4</td>
<td>background of 5.24 ppm</td>
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<tr>
<td>SF₆</td>
<td>SF⁺₅</td>
<td>127</td>
<td></td>
</tr>
<tr>
<td></td>
<td>SF⁺</td>
<td>51</td>
<td>interferes with R22 present at 7.6% of peak at mass 127</td>
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<tr>
<td>R22</td>
<td>CHF₂⁺</td>
<td>51</td>
<td>interferes with R13B1 or R14 present at 2.1% of peak at mass 51</td>
</tr>
<tr>
<td></td>
<td>CHCl⁺</td>
<td>69</td>
<td>interferes with R12 present at 1.5% of peak at mass 51</td>
</tr>
<tr>
<td></td>
<td>CCl⁺</td>
<td>85</td>
<td></td>
</tr>
<tr>
<td>R12</td>
<td>CCl₂⁺</td>
<td>85</td>
<td></td>
</tr>
<tr>
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<td>CF₃⁺</td>
<td>69</td>
<td></td>
</tr>
<tr>
<td>R12B2</td>
<td>CF₂Br⁺</td>
<td>120</td>
<td>not commonly available</td>
</tr>
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<td>n-Butane</td>
<td>C₄H₁₀⁺</td>
<td>58</td>
<td>flammable above 2%</td>
</tr>
<tr>
<td></td>
<td>C₅H₁⁺</td>
<td>43</td>
<td></td>
</tr>
<tr>
<td>Ne</td>
<td>Ne⁺</td>
<td>20</td>
<td>background of 18.18 ppm, expensive</td>
</tr>
<tr>
<td>Ar</td>
<td>Ar⁺</td>
<td>40</td>
<td>background of 1%, used as internal reference</td>
</tr>
</tbody>
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Note: Only the masses for the most abundant isotopes are listed.
Figure 1. Layout of the multitracer measurement system (MTMS)
Figure 2a. Flows to the bedroom

Flows To Bedroom
Volume = 61 m$^3$

Air Flow Rate [m$^3$/h]

From living room
From storage
From laundry
From outside
△ Total

Time of Day

12:00 00:00 12:00 00:00

Figure 2b. Flows to the living room

Flows To Living Room
Volume = 243 m$^3$

Air Flow Rate [m$^3$/h]

From bedroom
From storage
From laundry
From outside
△ Total

Time of Day

12:00 00:00 12:00 00:00

Figure 2c. Flows to the storage room

Flows To Storage Room
Volume = 60 m$^3$

Air Flow Rate [m$^3$/h]

From bedroom
From living room
From laundry
From outside
△ Total

Time of Day

12:00 00:00 12:00 00:00

Figure 2d. Flows to the laundry room

Flows To Laundry Room
Volume = 30 m$^3$

Air Flow Rate [m$^3$/h]

From bedroom
From living room
From storage
From outside
△ Total

Time of Day

12:00 00:00 12:00 00:00

Figure 2. Airflows from unoccupied house starting on December 24
Flows From Outside
House Volume = 473 m³

Flows From Bedroom (upper floor)
Volume = 150 m³

Flows From Living Area (upper floor)
Volume = 165 m³

Flows From Family Area (lower floor)
Volume = 157 m³

Figure 3a. Flows from outside

Figure 3b. Flows from the bedroom zone

Figure 3c. Flows from the living/kitchen zone

Figure 3d. Flows from the family/study zone

Figure 3. Airflows from occupied house on January 15 with a 30-minute analysis time
Figure 4. Airflows from occupied house on January 15 with a 10-minute analysis time